Running PyNN Simulations on SpiNNaker

Introduction
This manual will introduce you to the basics of using the PyNN neural network language on SpiNNaker
neuromorphic hardware.

Installation
The PyNN toolchain for SpiNNaker (sPyNNaker), can be installed by following the instructions available
from here:

http://spinnakermanchester.github.io/latest/spynnaker_install.html

Matplotlib is marked as optional, but you will also need to install this dependency to complete some of
the forthcoming exercises.

Spiking Neural Networks
Biological neurons have been observed to produce sudden and short increases in voltage, commonly
referred to as spikes. The spike causes a charge to be transferred across the synapse between neurons.
The charge from all the presynaptic neurons connected to a postsynaptic neuron builds up, until that
neuron releases the charge itself in the form of a spike. The spike travels down the axon of the neuron
which then arrives after some delay at the synapses of that neuron, causing charge to be passed forward to
the next neuron, where the process repeats.

1) Neurons “spike”, causing charge to be passed across the synapses between the neurons

2) When enough charge has been passed to the post-synaptic neuron, it causes it to spike

3) The spike travels down the axon of the neuron

Artificial spiking neural networks tend to model the membrane voltage of the neuron in response to the
incoming charge over time. The voltage is described using a differential equation over time, and the
solution to this equation is usually computed at fixed time-steps within the simulation. In addition to this, the
charge or current flowing across the synapse can also be modelled over time, depending on the model in
use.
The charge can result in either an excitatory response, in which the membrane voltage of the postsynaptic neuron increases or an inhibitory response, in which the membrane voltage of the postsynaptic neuron decreases as a result of the spike.

The PyNN Neural Network Description Language

PyNN is a language for building neural network models. PyNN models can then be run on a number of simulators without modification (or with only minor modifications), including SpiNNaker. The basic steps of building a PyNN network are as follows:

1. Setup the simulator
2. Create the neural populations
3. Create the projections between the populations
4. Setup data recording
5. Run the simulation
6. Retrieve and process the recorded data

An example of this is as follows:

try:
    import pyNN.spiNNaker as p
except:
    import spynnaker.pyNN as p

p.setup(timestep=1.0)
pop_1 = p.Population(1, p.IF_curr_exp, {}, label="pop_1")
input = p.Population(1, p.SpikeSourceArray,
    {'spike_times': [[0]]}, label="input")
input_proj = p.Projection(input, pop_1, p.OneToOneConnector(
    weights=5.0, delays=1), target="excitatory")
pop_1.record()
pop_1.record_v()
p.run(10)

spikes = pop_1.get_spikes()
v = pop_1.get_v()

import pylab
time = [i[1] for i in v if i[0] == 0]
membrane_voltage = [i[2] for i in v if i[0] == 0]
pylab.plot(time, membrane_voltage)
pylab.xlabel("Time (ms)")
pylab.ylabel("Membrane Voltage")
pylab.axis([0, 10, -75, -45])
pylab.show()

spike_time = [i[1] for i in spikes]
spike_id = [i[0] for i in spikes]
pylab.plot(spike_time, spike_id, ".")
pylab.xlabel("Time (ms)")
pylab.ylabel("Neuron ID")
pylab.axis([0, 10, -1, 1])
pylab.show()

This example runs using a 1.0ms timestep. It creates a single input source (A SpikeSourceArray) sending a single spike at time 0, connected to a single neuron (with model IF_curr_exp). The connection is weighted, so that a spike in the presynaptic neuron sends a current of 5 nanoamps (nA) to the excitatory synapse of the postsynaptic neuron, with a delay of 1 millisecond. The spikes and the membrane voltage are recorded, and the simulation is then run for 10 milliseconds. Graphs are then created of the membrane voltage and the spikes produced.
PyNN provides a number of standard neuron models. One of the most basic of these is known as the
Leaky Integrate and Fire (LIF) model, and this is used above (IF_curr_exp). This models the neuron as a
resistor and capacitor in parallel; as charge is received, this builds up in the capacitor, but then leaks out
through the resistor. In addition, a threshold voltage is defined; if the voltage reaches this value, a spike is
produced. For a time after this, known as the refractory period, the neuron is not allowed to spike again.
Once this period has passed, the neuron resumes operation as before. Additionally, the synapses are
modelled using an exponential decay of the received current input (5 nA in the above example); the weight
of the current is added over a number of timesteps, with the current decaying exponentially between each.
A longer decay rate will result in more charge being added overall per spike that crosses the synapse.

In the above example, the default parameters of the IF_curr_exp are used. These are:

'cm': 1.0,  # The capacitance of the LIF neuron in nano-Farads
'tau_m': 20.0,  # The time-constant of the RC circuit, in milliseconds
'tau_refrac': 0.1,  # The refractory period, in milliseconds
'v_reset': -65.0,  # The voltage to set the neuron at immediately after a spike
'v_rest': -65.0,  # The ambient rest voltage of the neuron
'v_thresh': -50.0,  # The threshold voltage at which the neuron will spike
'tau_syn_E': 5.0,  # The excitatory input current decay time-constant
'tau_syn_I': 5.0,  # The inhibitory input current decay time-constant
'i_offset': 0.0,  # A base input current to add each timestep

PyNN supports both current-based models and conductance-based models. In conductance models, the
input is measured in microSiemens, and the effect on the membrane voltage also varies with the current
value of the membrane voltage; the higher the membrane voltage, the more input is required to cause a
spike. This is modelled as the reversal potential of the synapse; when the membrane potential equals the
reversal potential, no current will flow across the synapse. A conductance-based version of the LIF model
is provided, which, in addition to the above parameters, also supports the following:

'e_rev_E': 0.,  # The reversal potential of the exponential synapse
'e_rev_I': -80.0  # The reversal potential of the inhibitory synapse

The initial value of the state variables of the neural model can also be set (such as the membrane voltage).
This is done via the initialize function of the population, which takes the name of the state variable as a
string (e.g. "v" for the membrane voltage), and the value to be assigned e.g. to set the voltage to -65.0mV:

pop.initialize("v", -65.0)

In PyNN, the neurons are declared in terms of a population of a number of neurons with similar properties.
The projection between populations therefore has a connector, which describes the connectivity between
the individual neurons in the populations. Some common connectors include:

- OneToOneConnector - each presynaptic neuron connects to one postsynaptic neuron (there should be
  the same number of neurons in each population) with weight weights and delay delays.
- AllToAllConnector - all presynaptic neurons connect to all postsynaptic neurons with weight weights
  and delay delays.
- FixedProbabilityConnector - each presynaptic neuron connects to each postsynaptic neuron with a
given fixed probability p_connect, with weight weights and delay delays.
- FromListConnector - the exact connectivity is described by conn_list, which is a list of
  (pre_synaptic_neuron_id, post_synaptic_neuron_id, weight, delay)

Commonly, random weights and/or delays are used. To specify this, the value of the weights or delays of
the connector are set to a RandomDistribution (note that the FromListConnector requires the specification
of explicit weights and delays, and so does not support this; instead the next() method of the random
distribution can be called to give random values for this connector). This supports several parameters via
the *parameters* argument, depending on the value of the *distribution* argument which identifies the distribution type. The supported distributions include a 'uniform' distribution, with parameters of [minimum value, maximum value]; and a 'normal' distribution with parameters of [mean, standard deviation]. A *boundary* can also be specified as [minimum, maximum] to constrain the values generated (where an unbounded end can make use of -numpy.inf or numpy.inf); this is often useful for keeping the delays within range allowed by the simulator. The *RandomDistribution* can also be used when specifying neural parameters, or when initialising state variables.

In addition to neuron models, the PyNN language also supports some utility models, which can be used to simulate inputs into the network with defined characteristics. These include:

- **SpikeSourceArray** - this sends spikes at predetermined intervals defined by *spike_times*. In general, PyNN forces each of the neurons in the population to spike at the same time, and so *spike_times* is an array of times, but sPyNNaker also allows *spike_times* to be an array of arrays, each defining the the times at which each neuron should spike e.g. *spike_times*=[[0], [1]] means that the first neuron will spike at 0ms and the second at 1ms.

- **SpikeSourcePoisson** - this sends spikes at random times with a mean rate of *rate* spikes per second, starting at time *start* (0.0ms by default) for a duration of *duration* milliseconds (the whole simulation by default).

### Using PyNN with SpiNNaker

In addition to the above steps, sPyNNaker requires the additional step of configuration via the .spynnaker.cfg file to indicate which physical SpiNNaker machine is to be used. This file is located in your home directory, and the following properties must be configured:

```
[Machine]
machineName      = None
version           = None
```

The *machineName* refers to the host or IP address of your SpiNNaker board. For a 4-chip board that you have directly connected to your machine, this is *usually* (but not always) set to 192.168.240.253, and the *version* is set to 3, indicating a “SpiNN-3” board (often written on the board itself). Most 48-chip boards are given the IP address of 192.168.240.1 with a *version* of 5.

The range of delays allowed when using sPyNNaker depends upon the timestep of the simulation. The range is 1 to 144 timesteps, so at 1ms timesteps, the range is 1.0ms to 144.0ms, and at 0.1ms, the range is 0.1ms to 14.4ms.

The default number of neurons that can be simulated on each core is 256; larger populations are split up into 256-neuron chunks automatically by the software. Note though that the cores are also used for other things, such as input sources, and delay extensions (which are used when any delay is more than 16 timesteps), reducing the number of cores available for neurons.

### Spike-Time-Dependent Plasticity

STDP plasticity is a form of learning that depends upon the timing between the spikes of two neurons connected by a synapse. It is believed to be the basis of learning and information storage in the human brain.

In the case where a presynaptic spike is followed closely by a postsynaptic spike, then it is presumed that the presynaptic neuron caused the spike in the postsynaptic neuron, and so the weight of the synapse between the neurons is increased. This is known as potentiation.
If a postsynaptic spike is emitted shortly before a presynaptic spike is emitted, then the presynaptic spike cannot have caused the postsynaptic spike, and so the weight of the synapse between the neurons is reduced. This is known as depression.

The size of the weight change depends on the relative timing of the presynaptic and postsynaptic spikes; in general, the change in weight drops off exponentially as the time between the spikes gets larger, as shown in the following figure [Sjöström and Gerstner (2010), Scholarpedia]. However, different experiments have highlighted different behaviours depending on the conditions (e.g. [Graupner and Brunel (2012), PNAS]). Other authors have also suggested a correlation between triplets and quadruplets of presynaptic and postsynaptic spikes to trigger synaptic potentiation or depression.

STDP in PyNN

The steps for creating a network using STDP are much the same as previously described, with the main difference being that some of the projections are given an `synapse_dynamics` argument to describe the plasticity. Here is an example of the creation of a projection with STDP:

```python

timing_rule = p.SpikePairRule(tau_plus=20.0, tau_minus=20.0)
weight_rule = p.AdditiveWeightDependence(
    w_max=5.0, w_min=0.0, A_plus=0.5, A_minus=0.5)

stdp_model = p.STDPMechanism(
    timing_dependence=timing_rule, weight_dependence=weight_rule)

stdp_projection = p.Projection(
    pre_pop, post_pop, p.OneToOneConnector(weights=0.0, delays=5.0),
    synapse_dynamics=p.SynapseDynamics(slow=stdp_model))
```

In this example, firstly the timing rule is created. In this case, it is a `SpikePairRule`, which means that the relative timing of the spikes that will be used to update the weights will be based on pairs of presynaptic and postsynaptic spikes. This rule has two required parameters, `tau_plus` and `tau_minus` which describe the respective exponential decay of the size of the weight update with the time between presynaptic and postsynaptic spikes. Note that the decay can be different for potentiation (defined by `tau_plus`) and depression (defined by `tau_minus`). This rule also accepts a parameter of `nearest` (by default this is `False`). If set to true, only the nearest pairs of spikes are considered when looking at weight updates.

The next thing defined is the weight update rule. In this case it is a `AdditiveWeightDependence`, which means that the weight will be updated by simply adding to the current weight. This rule requires the parameters `w_max` and `w_min`, which define the maximum and minimum weight of the synapse.
respectively, and the parameters $A_{\text{plus}}$ and $A_{\text{minus}}$ which define the maximum weight to respectively add during potentiation or subtract during depression. Note that the actual amount added or subtracted will depend additionally on the timing of the spikes, as determined by the timing rule.

In addition, there is also a $\text{MultiplicativeWeightDependence}$ supported, which means that the weight change depends on the difference between the current weight and $w_{\text{max}}$ for potentiation, and $w_{\text{min}}$ for depression. The value of $A_{\text{plus}}$ and $A_{\text{minus}}$ are then respectively multiplied by this difference to give the maximum weight change; again the actual value depends on the timing rule and the time between the spikes.

The timing and weight rules are combined into a single $\text{STDPMechanism}$ object which describes the overall desired mechanism. This is finally specified as the $\text{slow}$ argument of a $\text{SynapseDynamics}$ object, and then added to the $\text{Projection}$ using the $\text{synapse_dynamics}$ argument. Note that the projection still requires the specification of a $\text{Connector}$ which includes $\text{weights}$ and $\text{delays}$. This connector is still used to describe the overall connectivity between the neurons of the pre- and post-populations, as well as the delay values which are unchanged by the STDP rules, and the initial weight values. It is preferable that the initial weights fall between $w_{\text{min}}$ and $w_{\text{max}}$; it is not an error if they do not, but when the first update is performed, the weight will be changed to fall within this range.

$\text{Note}$: In the implementation of STDP on SpiNNaker, the plasticity mechanism is only activated when the second presynaptic spike is received at the postsynaptic neuron. Thus at least two presynaptic spikes are required for the mechanism to be activated.

**Task 1.1: A simple neural network [Easy]**

This task will create a very simple network from scratch, using some of the basic features of PyNN and SpiNNaker.

Write a network with a 1.0ms time step, consisting of two input source neurons connected to two current-based LIF neurons with default parameters, on a one-to-one basis, with a weight of 5.0 nA and a delay of 2ms. Have the first input neuron spike at time 0.0ms and the second spike at time 1.0ms. Run the simulation for 10 milliseconds. Record and plot the spikes received against time.

**Task 1.2: Changing parameters [Easy]**

This task will look at the parameters of the neurons and how changing the parameters will result in different network behaviour.

Using your previous script, set $\text{tau\_syn\_E}$ to 1.0 in the $\text{IF\_curr\_exp}$ neurons. Record the membrane voltage in addition to the spikes. Print the membrane voltage out after the simulation (you can plot it if you prefer, but you should note that the array returned from $\text{get\_v()}$ contains a list of $[\text{neuron\_id}, \text{time}, \text{voltage}]$ and so you will need to separate out the voltages of the individual neurons).

1. Did any of the neurons spike?
2. What was the peak membrane voltage of any of the neurons, compared to the default threshold voltage of -50mV?

Try increasing the weight of the connection and see what effect this has on the spikes and membrane voltage.

**Task 2.1: Synfire Chain [Moderate]**

This task will create a network known as a Synfire chain, where a neuron or set of neurons spike and cause activity in an ongoing chain of neurons or populations, which then repeats.

1. Setup the simulation to use 1ms timesteps.
2. Create an input population of 1 source spiking at 0.0ms.
3. Create a synfire population with 100 neurons.
4. With a FromListConnector, connect the input population to the first neuron of the synfire population, with a weight of 5nA and a delay of 1ms.
5. Using another FromListConnector, connect each neuron in the synfire population to the next neuron, with a weight of 5nA and a delay of 5ms.
6. Connect the last neuron in the synfire population to the first.
7. Record the spikes produced from the synfire populations.
8. Run the simulation for 2 seconds, and then retrieve and plot the spikes from the synfire population.

**Task 2.2: Random Values [Easy]**

Update the network above so that the delays in the connection between the synfire population and itself are generated from a uniform random distribution with values between 1.0 and 15.0. Update the run time to be 5 seconds.

**Task 3.1: Balanced Random Cortex-like Network [Hard]**

This task will create a network that this similar to part of the Cortex in the brain. This will take some input from outside of the network, representing other surrounding neurons in the form of poisson spike sources. These will then feed into an excitatory and an inhibitory network set up in a balanced random network. This will use distributions of weights and delays as would occur in the brain.

1. Set up the simulation to use 0.1ms timesteps.
2. Choose the number of neurons to be simulated in the network.
3. Create an excitatory population with 80% of the neurons and an inhibitory population with 20% of the neurons.
4. Create excitatory poisson stimulation population with 80% of the neurons and an inhibitory poisson stimulation population with 20% of the neurons, both with a rate of 1000Hz.
5. Create a one-to-one excitatory connection from the excitatory poisson stimulation population to the excitatory population with a weight of 0.1nA and a delay of 1.0ms.
6. Create a similar excitatory connection from the inhibitory poisson stimulation population to the inhibitory population.
7. Create an excitatory connection from the excitatory population to the inhibitory population with a fixed probability of connection of 0.1, and using a normal distribution of weights with a mean of 0.1 and standard deviation of 0.1 (remember to add a boundary to make the weights positive) and a normal distribution of delays with a mean of 1.5 and standard deviation of 0.75 (remember to add a boundary to keep the delays within the allowed range on SpiNNaker).
8. Create a similar connection between the excitatory population and itself.
9. Create an inhibitory connection from the inhibitory population to the excitatory population with a fixed probability of connection of 0.1, and using a normal distribution of weights with a mean of -0.4 and standard deviation of 0.1 (remember to add a boundary to make the weights negative) and a normal distribution of delays with a mean of 0.75 and standard deviation of 0.375 (remember to add a boundary to keep the delays within the allowed range on SpiNNaker).
10. Create a similar connection between the inhibitory population and itself.
11. Initialize the membrane voltages of the excitatory and inhibitory populations to a uniform random number between -65.0 and -55.0.
12. Record the spikes from the excitatory population.
13. Run the simulation for 1 or more seconds.
14. Retrieve and plot the spikes.
The graph should show what is known as Asynchronous Irregular spiking activity - this means that the neurons in the population don’t spike very often and when they do, it is not at the same time as other neurons in the population.

**Task 3.2: Network Behavior [Moderate]**

Note in the above network that the weight of the inputs is the same as the mean weight of the excitatory connections (0.1nA) and that the mean weight of the inhibitory connections is 4 times this value (-0.4nA). Try setting the excitatory connection mean weight and input weights to 0.11nA and the inhibitory mean weight to -0.44nA, and see how this affects the behavior. What other behavior can you get out of the network by adjusting the weights?

**Task 4.1: STDP Network [Easy]**

This task will create a simple network involving STDP learning rules.

Write a network with a 1.0ms time step consisting of two single-neuron populations connected with an STDP synapse using a spike pair rule and additive weight dependency, and initial weights of 0. Stimulate each of the neurons with a spike source array with times of your choice, with the times for stimulating the first neuron being slightly before the times stimulating the second neuron (e.g. 2ms or more), ensuring the times are far enough apart not to cause depression (compare the spacing in time with the tau_plus and tau_minus settings); note that a weight of 5.0 should be enough to force an IF_curr_exp neuron to fire with the default parameters. Add a few extra times at the end of the run for stimulating the first neuron. Run the network for a number of milliseconds and extract the spike times of the neurons and the weights.

You should be able to see that the weights have changed from the starting values, and that by the end of the simulation, the second neuron should spike shortly after the first neuron.

**Task 4.2: STDP Parameters [Easy]**

Alter the parameters of the STDP connection, and the relative timing of the spikes. Try starting with a large initial weight and see if you can get the weight to reduce using the relative timing of the spikes.

**Task 5: STDP Curve [Hard]**

This task will attempt to plot an STDP curve, showing how the weight change varies with timing between spikes.

1. Set up the simulation to use a 1ms time step.
2. Create a population of 100 presynaptic neurons.
3. Create a spike source array population of 100 sources connected to the presynaptic population. Set the spikes in the arrays so that each spikes twice 200ms apart, and that the first spike for each is 1ms after the first spike of the last e.g. [[0, 200], [1, 201], …] (hint: you can do this with a list comprehension).
4. Create a population of 100 postsynaptic neurons.
5. Create a spike source array connected to the postsynaptic neurons all spiking at 50ms.
6. Connect the presynaptic population to the postsynaptic population with an STDP projection with an initial weight of 0.5 and a maximum of 1 and minimum of 0.
7. Record the presynaptic and postsynaptic populations.
8. Run the simulation for long enough for all spikes to occur, and get the weights from the STDP projection.
9. Draw a graph of the weight changes from the initial weight value against the difference in presynaptic and postsynaptic neurons (hint: the presynaptic neurons should spike twice but the
postsynaptic should only spike once; you are looking for the first spike from each presynaptic neuron).